

ENGINEERING PHYSICS

1st SEM

MECHANICAL ENGG.

Under SCTE&VT,Odisha

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⇒ What is science?
The systematic knowledge earned through observation, experiment and logic is known as science.

⇒ The word science is derived from Latin word "scientia" which means "to know".

⇒ Science is divided into two types

(1) Physical science

(2) Biological science

Physical science

⇒ The branches of science which deals with non-living things is called as Physical science.

EX:- Physics, Chemistry, Engineering etc.

Biological science

⇒ The branch of science which deals with life is called as Biological science.

EX:- Botany, Zoology, Medical science etc.

⇒ What is physics?

It is the science of nature which describes laws or principles that explain how natural world works.

⇒ The word physics is derived from a Greek word "PHYSIS" which means "nature".

⇒ It deals with matter and energy around us.

- ⇒ It deals with chapters like
- (1) mechanics
 - (2) heat and thermodynamics
(cheats motion)
 - (3) Electricity
 - (4) Optics
 - (5) Nuclear physics
 - (6) Atomic physics

⇒ Physical quantity can be measured
Anything which can be measured
and in terms of which laws of
physics are expressed is called
physical quantity

EX:- mass, length, time, force, velocity,
speed, energy etc.

⇒ Physical quantities are of two types

- (1) Fundamental physical quantities
- (2) Derived "

Fundamental quantities

⇒ The physical quantities those which
can be measured directly are
called fundamental quantities

OR
⇒ The physical quantities which
do not depend on others to be
measured is known as fundamental
quantities.

EX: - mass, length, time, electric current, Temperature, Luminous intensity, amount of substance.

Derived quantities

The physical quantities which depend on fundamental quantities to be measured are called derived quantities.

EX: - Force, Power, acceleration, volume, area etc.

magnitude of Physical quantities

~~The physical quantities which depend on fundamental quantities to be measured~~

It is the product of a number and a unit

mathematically, $m = nu$

where n = number

u = unit of the physical quantity

For a physical quantity

$$n_1 u_1 = n_2 u_2$$

where n_1 and u_1 are number and unit of 1st system

$$\text{1 m} = 10^3 \text{ cm}$$

n_1 and u_1 are numbers and unit in ~~SI~~ and system

$$1\text{m} = 100\text{cm}$$

$$\downarrow \quad \downarrow \quad \downarrow$$
$$n_1 u_1 \quad n_2 u_2$$

⇒ For a physical quantity

$$\boxed{n \alpha \frac{1}{u}}$$

⇒ Unit
A constant quantity (value) in terms of which other quantities are expressed is called unit

OR
⇒ A standard of measurement may be called a unit.

Ex: - meter, kilogram, centimeter, kilogram second etc.

⇒ Standard or standard unit
An internationally accepted and well defined symbol use to measure physical quantities is called standard unit.

Ex: - standard of mass kilogram,
standard of length meter,
standard of time second

Multiples and sub-multiple of units

Multiples			Sub-multiples		
Prefix	Symbol	value	Prefix	Symbol	value
deca	da	10^1	deci	d	10^{-1}
hecto	h	10^2	centi	c	10^{-2}
kilo	k	10^3	milli	m	10^{-3}
mega	M	10^6	micro	μ	10^{-6}
giga	G	10^9	nano	n	10^{-9}
tera	T	10^{12}	pico	p	10^{-12}
peta	P	10^{15}	femto	f	10^{-15}
exa	E	10^{16}	atto	a	10^{-18}

EXAMPLES

⇒ multiple units of length
deca meter, hectometer, tera meter

⇒ multiple units of mass
deca gram, hecto gram, tera gram

⇒ multiple units of time
deca second, hectosecond, tera second

⇒ sub-multiple units of length
decimeter, centimeter, micrometer

⇒ sub-multiple units of mass
centigram, microgram, milligram

⇒ sub-multiple units of time
centisecond, millisecond, microsecond

Types of unit

⇒ There are four types of units

- (1) Fundamental units
 - (2) Derived units
 - (3) Supplementary units
 - (4) Practical units
- Fundamental units

⇒ The units of fundamental quantities are called fundamental units

EX:- meter, kg, second, centimeter, gram etc.

Derived units

⇒ The units of derived quantities are called derived units.

EX:- ~~meter~~ m/s (speed), m/s^2 (acceleration), ~~newton~~ newton (force), joule etc.

Supplementary unit

⇒ The units of supplementary quantities (plane angle and solid angle) are called supplementary units (a)

EX:- unit of plane angle - radian.
symbol - rad
EX:- degree, radian

$$1 \text{ light year} = 9.46 \times 10^{15} \text{ m}$$

unit of solid angle - steradian

symbol - Sr

Practical units

⇒ The units which are neither fundamental nor derived and have a special name and are used in our day today life are called practical units.

EX: Light year

(1) Light year

⇒ It is a bigger practical unit of length

⇒ definition - It is the distance traveled by light in vacuum in one year at its speed.

$$v = \frac{s}{t} \Rightarrow s = vt$$

$$1 \text{ ly} = 9.46 \times 10^{15} \text{ m}$$

$$1 \text{ ly} = s = vt = (3 \times 10^8 \text{ m/s}) \times 1 \text{ year}$$

$$= 3 \times 10^8 \text{ m/s} \times 365 \times 24 \times 3600 \text{ s}$$

$$= 9.46 \times 10^{15} \text{ m}$$

$$= 9.46 \text{ Pm}$$

(2) Astronomical unit (A.U)

⇒ It is a bigger practical unit of length

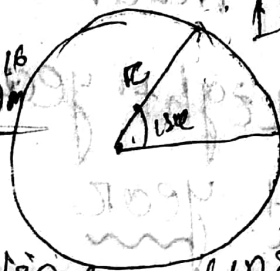
Astronomical Unit

⇒ It is the average distance between Sun and the Earth.

$$1 \text{ A.U.} = 1.496 \times 10^{11} \text{ m}$$

⇒ Parsec (par sec) is defined as the distance at which an arc of 1 A.U. subtends an angle of 1 second.

$$1 \text{ par sec} = 3.084 \times 10^{16} \text{ m}$$



⇒ It is a bigger practical unit of length (macroscopic)

Angstrom (Å)

⇒ It is a smaller (microscopic) unit of length.

$$1 \text{ Å} = 10^{-10} \text{ m}$$

micron (μm)

⇒ It is a smaller practical unit of length.

$$1 \mu\text{m} = 10^{-6} \text{ m}$$

Femtometre (fm)

⇒ It is a smaller practical unit of length.

$$1 \mu\text{m} = 10^{-15} \text{ m}$$

A.M.U (Atomic mass unit/u)

⇒ It is a smaller practical unit of mass

$$1 \text{ u} = 1.66 \times 10^{-27} \text{ kg}$$

Characteristics of standard unit

1) It should be invariable (not change with place and time)

2) It should be indestructible (not change with temperature and pressure)

3) It should be accessible (easily available)

4) It should be reproducible

5) It should be universal

5) It should be internationally accepted

⇒ Find the relation between a light year and astronomical

Unit

Solution

$$1 \text{ ly} = 9.46 \times 10^{15} \text{ m} \quad \text{--- (i)}$$

$$\therefore 1 \text{ m} = \frac{1 \text{ ly}}{9.46 \times 10^{15}} \quad \text{--- (ii)}$$

$$1 \text{ A.U} = 1.496 \times 10^{11} \text{ m} \quad \text{--- (ii)}$$

$$\therefore 1 \text{ m} = \frac{1 \text{ A.U}}{1.496 \times 10^{11}} \quad \text{--- (ii)}$$

For eq (i) and (ii)

$$\frac{1 \text{ ly}}{9.46 \times 10^{15}} = \frac{1 \text{ A.U}}{1.496 \times 10^{11}}$$

OR

$$1 \text{ ly} = \frac{1 \text{ A.U.} \times 9.46 \times 10^{15}}{1.496 \times 10^{11}}$$

$$1 \text{ ly} = \frac{1 \text{ A.U.} \cdot 9.46 \times 10^{15}}{1.496}$$

$$1 \text{ ly} = \frac{9.46 \times 10^4 \text{ A.U.}}{1.496}$$

$$1 \text{ ly} = 6.328 \times 10^4 \text{ A.U.}$$

(2) Find relation between parsec and astronomical unit.

$$1 \text{ parsec} = 3.084 \times 10^{16} \text{ m} \quad \text{--- (i)}$$

$$1 \text{ m} = \frac{3.084 \times 10^{16}}{1.496 \times 10^{11}} \text{ A.U.} \quad \text{--- (ii)}$$

$$\Rightarrow 1 \text{ m} = \frac{207.1 \text{ A.U.}}{1.496 \times 10^{11}} \quad \text{--- (ii)}$$

From equation (i) and (ii)

$$\frac{1 \text{ parsec}}{3.084 \times 10^{16}} = \frac{1 \text{ A.U.}}{1.496 \times 10^{11}}$$

$$\Rightarrow 1 \text{ parsec} = \frac{3.084 \times 10^{16} \text{ A.U.}}{1.496 \times 10^{11}}$$

$$\Rightarrow 1 \text{ parsec} = \frac{3.084 \text{ A.U.}}{1.496} \times 10^{16-11}$$

$$1 \text{ parsec} = \frac{3.084 \text{ AU}}{1.496} \times 10^5$$

$$\Rightarrow 1 \text{ parsec} = 2.06 \times 10^5 \text{ AU}$$

$$1 \text{ parsec} = 3.258 \times 10^7 \text{ light years}$$

(3) How many nano meters are there in Pico meter?

$$1 \text{ Pico meter} = 10^{-12} \text{ m} \quad (i)$$

$$\therefore 1 \text{ meter} = \frac{10^{12} \text{ pm}}{1} \quad (ii)$$

$$1 \text{ nm} = 10^{-9} \text{ m} \quad (iii)$$

$$\therefore 1 \text{ m} = \frac{1 \text{ nm}}{10^{-9}} \quad (iv)$$

From eqⁿ (i) and (iv):

$$\frac{1 \text{ pm}}{10^{-12}} = \frac{1 \text{ nm}}{10^{-9}}$$

$$\Rightarrow \text{pm} = \frac{1 \text{ nm} \times 10^{-12}}{10^{-9}}$$

$$\Rightarrow \text{pm} = 10^{-12+9} = 10^{-3} = 10^{-3} \text{ nm}$$

$\therefore 10^{-3} \text{ nm}$ are present in 1 pm.

(4) How many tera meters are there in one mega meter?

$$1 \text{ mega meter} = 10^6 \text{ m}$$

$$1 \text{ tera meter} = 10^{12} \text{ m}$$

$$\frac{1 \text{ m}}{1 \text{ Tm}} = \frac{10^6}{10^{12}} = 10^{-6} \text{ megameter} = 10^{-6} \text{ m}$$

(5) How many micrometers are there in one gigameter?

$$1 \text{ gigameter} = 10^9 \text{ m}$$

$$\therefore 1 \text{ m} = \frac{1 \text{ gm}}{10^9} = 10^{-9} \text{ gm} \quad \text{--- (i)}$$

$$1 \text{ micrometer} = 10^{-6} \text{ m}$$

$$\therefore 1 \text{ m} = \frac{1 \text{ }\mu\text{m}}{10^{-6}} = 10^6 \text{ }\mu\text{m} \quad \text{--- (ii)}$$

From eqⁿ (i) and (ii)

$$\cancel{1 \text{ gm}} \quad 10^{-9} \text{ gm} = 10^6 \text{ }\mu\text{m}$$

$$\Rightarrow 1 \text{ gm} = \frac{10^6 \text{ }\mu\text{m}}{10^{-9}}$$

$$\Rightarrow 1 \text{ gm} = 10^{6+9} \text{ }\mu\text{m}$$

$$\Rightarrow 1 \text{ gm} = 10^{15} \text{ }\mu\text{m}$$

System of units

⇒

There are four types of system of unit.

- (1) M.K.S system
- (2) C.G.S system
- (3) F.P.S system
- (4) S.I system (International system)

S.I system of unit

⇒

M.K.S system could not cover whole/all branches of physics so in 1971 a conference on weights and measures decided a new system of units which is called International system of units.

⇒ Shortly it is represented S.I unit according to French name "Le Systeme International d'units"

⇒ This system contains seven fundamental units and two supplementary units

S.I Fundamental units

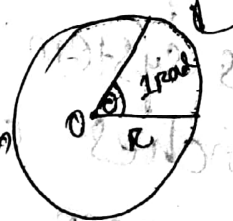
- (i) meter (m) - unit of length
- (ii) kilogram (kg) - unit of mass
- (iii) second (s) - unit of time
- (iv) Kelvin (K) - unit of temperature

- (v) ampere - (A) unit of ^{electric} current
- (vi) Candela - (cd) unit of luminous intensity
- (vii) mole - (mol) - unit of amount of substances

Supplementary units

- (i) radian (rad) - unit of plane angle
- (ii) Steradian (sr) - unit of solid angle

⇒ one radian is defined as the unit of plane angle subtended at the centre of a circle by an arc whose magnitude is equal to the radius.



when $l = r$, $\theta = \frac{l}{r} = \frac{r}{r} = 1$ radian

steradian

⇒ 1 steradian is defined as the solid angle subtended at the centre of a sphere



is equal to the square magnitude
 square of the magnitude of
 its radius

when surface area $(A) = (\text{radius})^2$

$$\omega = \frac{\text{surface area}}{(\text{radius})^2} = \frac{\text{radius}^2}{\text{radius}^2}$$

$\Rightarrow \omega = 1$ steradian

\Rightarrow Total solid angle / maximum
 solid angle subtended at the
 centre of the sphere is 4π sr

$$\omega = \frac{S.A}{(\text{radius})^2} = \frac{4\pi R^2}{R^2} = 4\pi$$

Advantages of s.?

- \Rightarrow It is an absolute system
- \Rightarrow It is a coherent system of unit.
- \Rightarrow It is a rational system of unit.
(rational)
(creative & effective)
or sensible
- \Rightarrow It is a metric system.
(10⁹ 2000)

Dimension of Physical quantity

(nature)
Dimensions of a physical quantity are defined as the powers to which fundamental quantities are raised to represent the nature of the physical quantities.

Length has dimension $[L]$

mass has dimension $[M]$

Time " " $[T]$

Temp " " $[K]$

Electric current " " $[A]$

Luminous intensity " " $[cd]$

Amount of substance " " $[mol]$

Dimensions of speed

$$\text{Speed} = \frac{\text{Distance}}{\text{Time}} = \frac{[L]}{[T]}$$

$$\therefore \frac{\text{Length}}{\text{Time}} = \frac{L}{T} = [L^1 T^{-1}]$$

Thus, speed has 1 dimension in length and -1 dimension in time and "0" dimension in mass.

Q. i.e. $(0, 1, -1)$
 $\frac{M}{L} \cdot \frac{L}{T}$

⇒ Dimension of acceleration

$$\text{acceleration} = \frac{\text{velocity}}{\text{time}}$$

$$= \frac{\text{Displacement}}{\text{time}} = \frac{\text{Length}}{\text{Time}}$$

$$= \frac{\frac{L}{T}}{T} = \frac{L}{T} \times \frac{1}{T} = \frac{L}{T^2} = [L^1 T^{-2}]$$

$$= [M^0 L^1 T^{-2}]$$

Thus acceleration has 1 dimension in length and, -2 dimension in time and "0" dimension in mass.

(4) Dimension of Force

$$F = ma$$

$$= \text{mass} \times \frac{\text{velocity}}{\text{time}}$$

$$= \text{mass} \times \frac{\text{Displacement}}{\text{time}^2}$$

$$= M \times \frac{L}{T^2} = \frac{ML}{T^2} = MLT^{-2}$$

$$= [M^1 L^1 T^{-2}]$$

Thus force has 1 dimension in mass and, 1 dimension in length and, -2 dimension in time. i.e. $[M^1 L^1 T^{-2}]$

→ Dimension of work

8→

$$\begin{aligned} \text{Energy/Work} &= FS \\ &= [M^1 L^1 T^{-2}] [L] \\ &= [M^1 L^2 T^{-2}] \end{aligned}$$

Thus work has 1 dimension in mass and, 2 dimension in length

→ Dimension of energy

Energy = same as work
i.e. $[M^1 L^2 T^{-2}]$

9-

Thus energy has 1 dimension in mass and, 2 dimension in length and, -2 dimension in time

Dimension of momentum

$$\text{momentum} = mv \text{ @ } \text{mass}$$

$$= [M] [L^1 T^{-1}]$$

$$= [M^1 L^1 T^{-1}]$$

Thus momentum has 1 dimension in mass, and 1 di

8 →

~~Area~~ Dimension of Area

$$\text{Area} = \text{Length} \times \text{breadth}$$

$$= [L][L]$$

$$= [L^2]$$

$$= [M^0 L^2 T^0]$$

Thus area has '0' dimension in ~~length~~^{mass} and, 2 dimension in length

9 → Dimension of volume

$$\text{Volume} = \text{Length} \times \text{breadth} \times \text{height}$$

$$= L \times L \times L$$

$$= [L^3]$$

$$= [M^0 L^3 T^0]$$

Thus volume has '0' dimension in mass and, 3 dimension in length and '0' dimension in time.

10 → Dimension of kinetic energy

$$E_k = \frac{1}{2} m v^2$$

$$= M(LT^{-1})^2 = [M^1 L^2 T^{-2}]$$

~~Thus~~

10 → Dimension of potential energy

$$E_p = mgh = [M^1 L^1 T^{-2} \cdot L] = [M^1 L^2 T^{-2}]$$

Important points/tools in dimensions

Dimensional formula

Dimensional formula of

$$\text{Speed is } [\text{Speed}] = [M^0 L^1 T^{-1}]$$

$$[\text{Force}] = [M^1 L^1 T^{-2}] \text{ etc}$$

Dimensional equation

$$[\text{Speed}] = [M^0 L^1 T^{-1}] \text{ etc.}$$

Dimensions gives the nature of a physical quantity and also gives the unit of physical quantity \Rightarrow

Dimension of a physical quantity doesn't give its magnitude \Rightarrow

\Rightarrow 1, 2, 3, ... have no dimension. \Rightarrow

$$[1] = [M^0 L^0 T^0]$$

$$[2] = [M^1 L^1 T^0]$$

\Rightarrow π has no dimensions \Rightarrow

$$[\pi] = [M^0 L^0 T^0]$$

⇒ Angle has no dimension
i.e. dimensionless quantity

$$[\text{angle}] = [\theta] = \left[\frac{l}{r} \right] = \left[\frac{L}{L} \right] = [1] = [M^0 L^0 T^0]$$

⇒ $\sin \theta$, $\cos \theta$, $\tan \theta$, $\sec \theta$
have no dimension.

$$[\sin \theta] = \left[\frac{p}{h} \right] = \left[\frac{L}{L} \right] = [1] = [M^0 L^0 T^0]$$

⇒ $\log u$ has no dimension
where $n = 1, 2, 3, 4$

$$[\log u] = [M^0 L^0 T^0]$$

⇒ e^n has no dimension

$$[e^n] = [M^0 L^0 T^0]$$

where $e =$ Irrational number

⇒ Dimensional variables

meaning:- (i) which have dimensions
(ii) whose magnitude are variable.

EX:- speed, velocity, acceleration,
Force etc.

⇒ Dimensional Constant

meaning:- (i) which have dimensions
(ii) whose magnitude are constant.

EX:- speed of light in vacuum ($3 \times 10^8 \text{ m/s}$),
Gravitational constant (G) (6.67×10^{-11})

Nm^2/kg^2

Non-Dimensional Variable

- meaning: (i) which have no dimension
(ii) whose magnitudes are variable

EX: - Angle

Non-Dimensional Constant

- meaning: (i) which have no dimension
(ii) whose magnitudes are constant

EX: - $\pi, 1, 2, 3, 4, \dots$

Principle of homogeneity of dimension

- \Rightarrow A physical equation is dimension correct if all terms of the equation have same dimension.

Physical quantities can be added or subtracted if they have same dimensions

EX: -

- The position of a particle changes with time is given by $x = a + bt + ct^2$

where a, b, c are constants.

find dimensional formula of a, b and c .

according to the principle of homogeneity

of dimension

$$[a] = [x] = [L] = [m^0 L^1 T^0]$$

$$[bt] = x \text{ or } b = \left[\frac{x}{t}\right] = \left[\frac{L}{T}\right] = [L T^{-1}]$$

$$[ct^2] = [x] \text{ or } [c] = \left[\frac{x}{t^2}\right] = \left[\frac{L}{T^2}\right] = [LT^{-2}]$$

1) The position of a particle is given by

$$x = a - bt - ct^2$$

where a, b, c are constant

t = time in second

x = distance in meter

Find the dimension of a, b and c .

Solution

According to the principle of homogeneity of dimension.

$$[a] = [x] = [L] = [m^0 L^1 T^0] = \text{meter (unit)}$$

$$[bt] = [x] \text{ or } [b] = \left[\frac{x}{t}\right] = \left[\frac{L}{T}\right] = [m^0 L^1 T^{-1}] = \text{meter/sec}$$

$$[ct^2] = [x] \text{ or } [c] = \left[\frac{x}{t^2}\right] = \left[\frac{L}{T^2}\right] = [m^0 L^1 T^{-2}] = \text{meter/sec}^2$$

Speed is given by $v = at + \frac{b}{(c+t)}$

where t = time

Find $[a], [b], [c]$

Solution

$$[at] = [v] \text{ or } [a] = \left[\frac{v}{t}\right] = \left[\frac{LT^{-1}}{T}\right] = [LT^{-2}]$$

$$[v] = \left[\frac{b}{c+t}\right] \text{ or } [b] = [v][c+t] = [LT^{-1}][T] = [L]$$

$$[c] = [T]$$

An ideal gas equation is given by

$$\left(P + \frac{a}{v^2}\right)(v-b) = Rt$$

where P = Pressure

v = volume

Find $[a], [b]$

Solution

According to the principle of homogeneity

$$[P] = \left[\frac{a}{v^2} \right]$$

$$\Rightarrow [a] = [P][v^2] = [m^1 L^{-1} T^{-2}] [L^2] \quad (1)$$

$$[a] = [m^2 L^1 T^{-2}]$$

$$[v] = [L]$$

$$\Rightarrow [b] = [L^3]$$

(5) Force is given by $F = at + bt^2$
where $t = \text{time}$
Find $[a]$ and $[b]$

Solution

$$[F] = [at] = \frac{[m^1 L^1 T^{-2}]}{[T]} = [m^1 L^1 T^{-3}]$$

$$[a] = \frac{[F]}{[t]} = \frac{[m^1 L^1 T^{-3}]}{[T]} = [m^1 L^1 T^{-4}]$$

$$[F] = [bt^2] \text{ or } [b] = \frac{[F]}{[t^2]} = \frac{[m^1 L^1 T^{-3}]}{[T^2]} = [m^1 L^1 T^{-5}]$$

$$[b] = [m^1 L^1 T^{-5}]$$

2) If $y = a \sin(\omega t - kx)$

find $\left[\frac{\omega}{k} \right]$

where $t = \text{time}$
 $x = \text{displacement}$

Sine $[a] = [m^0 L^1 T^0]$

$$[\omega t] = [m^0 L^1 T^0]$$

$$[kx] = [m^0 L^1 T^0]$$

or $[x] = [L] = [L] = [L T^{-1}]$

⑦ Find dimensional formula of 'n' in e^{-2nt}

where t = time

$$[e^{-2nt}] = [M^0 L^0 T^0]$$

$$\therefore [-2nt] = [M^0 L^0 T^0]$$

$$\therefore [n] = \frac{[M^0 L^0 T^0]}{[t]} = [M^0 L^0 T^{-1}]$$

⑧ The position of a particle changes with time 't'. $s(t)$ is given by as given by $s(t) = \frac{v_0}{\alpha} (1 - e^{-\alpha t})$

by $s(t) = \frac{v_0}{\alpha} (1 - e^{-\alpha t})$

find $[\alpha]$ and $[v_0]$

$$s(t) = \frac{v_0}{\alpha} (1 - e^{-\alpha t}) = \frac{v_0}{\alpha} - \frac{v_0}{\alpha} e^{-\alpha t}$$

~~$$\left[\frac{v_0}{\alpha}\right] = [s] \quad [v_0] = [s][\alpha]$$~~

$$[-\alpha t] = [M^0 L^0 T^0]$$

$$[\alpha] = \frac{[M^0 L^0 T^0]}{[t]} = \frac{[M^0 L^0 T^0]}{[T]} = [M^0 L^0 T^{-1}]$$

~~$$[s] \left[\frac{v_0}{\alpha}\right] = [s] \text{ or } [v_0] = [s][\alpha]$$~~

$$[v_0] = [L][T^{-1}] = [M^0 L^1 T^{-1}]$$

Uses of Dimensional or Dimensional Analysis

(i) Dimensional Analysis is used to convert a unit from one system to another system.

Problem - 1

convert one Newton into dyne by dimension.

$$[F] = [M^1 L^1 T^{-2}]$$

where $n_1 u_1 = n_2 u_2$

$$n_1 [M_1 L_1 T_1^{-2}] = n_2 [M_2 L_2 T_2^{-2}]$$

$1 \text{ N} = ? \text{ dyne}$

$$n_2 = \frac{n_1 [M_1 L_1 T_1^{-2}]}{[M_2 L_2 T_2^{-2}]}$$

$$\text{or } n_2 = n_1 \left[\frac{M_1}{M_2} \right]^1 \left[\frac{L_1}{L_2} \right]^1 \left[\frac{T_1}{T_2} \right]^{-2}$$

$$= n_1 \left[\frac{\text{kg}}{\text{g}} \right] \times \left[\frac{\text{m}}{\text{cm}} \right] \left[\frac{\text{sec}}{\text{sec}} \right]^{-2}$$

$$= n_1 \left[\frac{1000 \text{g}}{\text{g}} \right] \times \left[\frac{100 \text{cm}}{\text{cm}} \right]$$

$$= 100000 \times 100$$

$$= 10^5$$

(2)	<u>M.K.S (system-1)</u>	<u>Physical quantity</u>	<u>C.G.S (system-2)</u>
	$m_1 = 1 \text{ kg}$	Force	$m_2 = 1 \text{ g}$
	$L_1 = 1 \text{ m}$	$a = 1$	$L_2 = 1 \text{ cm}$
	$T_1 = 1 \text{ sec}$	$b = 1$	$T_2 = 1 \text{ sec}$
	$n_1 = 1$	$c = 1$	$n_2 = ?$

Physical quantity of system-1

$$= n_1 [m_1^a L_1^b T_1^c]$$

Physical quantity of system-2

$$= n_2 [m_2^a L_2^b T_2^c]$$

AS the physical quantity are same for both the system so.

$$n_1 [m_1^a L_1^b T_1^c] = n_2 [m_2^a L_2^b T_2^c]$$

$$\Rightarrow n_2 = n_1 \frac{[m_1^a L_1^b T_1^c]}{[m_2^a L_2^b T_2^c]} = n_1 \left[\frac{m_1}{m_2} \right]^a \left[\frac{L_1}{L_2} \right]^b \left[\frac{T_1}{T_2} \right]^c$$

$$\Rightarrow n_2 = 1 \left[\frac{1 \text{ kg}}{1 \text{ g}} \right]^1 \left[\frac{1 \text{ m}}{1 \text{ cm}} \right]^1 \left[\frac{1 \text{ sec}}{1 \text{ sec}} \right]^1$$

$$\Rightarrow n_2 = \left[\frac{1000 \text{ g}}{1 \text{ g}} \right] \left[\frac{100 \text{ cm}}{1 \text{ cm}} \right] \left[\frac{1 \text{ sec}}{1 \text{ sec}} \right]$$

$$\Rightarrow n_2 = 1000 \times 100 = 10^5$$

1 Newton = 10^5 dyne.

(3) Convert 10 Joule into erg by dimension

(3)	<u>M.K.S (1st system)</u>	<u>P.W</u>	<u>C.G.S (2nd system)</u>
	$m_1 = 1 \text{ kg}$	$a = 1$	$m_2 = 1 \text{ g}$
	$L_1 = 1 \text{ m}$	$b = 2$	$L_2 = 1 \text{ cm}$
	$T_1 = 1 \text{ sec}$	$c = -2$	$T_2 = 1 \text{ sec}$
	$n_1 = 10$		$n_2 = ?$

putting these in eqn (1)

$$n_2 = 10 \left[\frac{1 \text{ kg}}{1 \text{ g}} \right]^1 \left[\frac{1 \text{ m}}{1 \text{ cm}} \right]^2 \left[\frac{1 \text{ sec}}{1 \text{ sec}} \right]^{-2}$$

$$= 10 \times \left[\frac{1000 \text{ g}}{9} \right] \left[\frac{1000 \text{ cm}^2}{\text{cm}^2} \right] \left[\frac{1 \text{ sec}}{1 \text{ sec}} \right]^2$$

$$= 10 \times 1000 \times 10000 \times \frac{1}{1} = 10^8 \text{ erg}$$

$$= 10^8 \text{ erg}$$

express 100 joule work in a system where fundamental unit are meter and second

(S)

(SI) MKS
MKS

$m_1 = 1 \text{ kg}$
 $L_1 = 1 \text{ m}$
 $T_1 = 1 \text{ sec}$
 $n_1 = 100$

PA
work
 $a = 1$
 $b = 2$
 $c = -2$

2nd system
 $n_2 = ?$
 $m_2 = 50 \text{ g}$
 $L_2 = 10 \text{ cm} = 10 \times 10^{-2} \text{ m} = 10^{-1} \text{ m}$
 $T_2 = 5 \text{ sec}$

$$n_2 = n_1 \left[\frac{m_1}{m_2} \right] \left[\frac{L_1}{L_2} \right] \left[\frac{T_1}{T_2} \right]^a$$

$$= 100 \left[\frac{1 \text{ kg}}{50 \text{ g}} \right] \left[\frac{1 \text{ m}}{10^{-1} \text{ m}} \right] \left[\frac{1 \text{ sec}}{5 \text{ sec}} \right]^2$$

$$= 100 \times \left[\frac{10^3 \text{ g}}{5 \times 10^1 \text{ g}} \right] \left[\frac{10^2 \text{ cm}^2}{10^1 \text{ cm}^2} \right] \left[\frac{1}{5} \right]^2$$

~~$$= 100 \times 20 \times 10^2$$~~

$$= 100 \times \left[\frac{10^2}{5} \right] \left[\frac{1}{10} \right]^2 \left[5^{-2} \right]$$

$$= 100 \times 20 \times \frac{1}{100} \times \frac{1}{25} = \frac{2000}{25} = 80$$

use-2

dimensional analysis is used to check the correctness of a physical equation

(1) check the correctness of $v = u + at$

$$\text{where } v = I \cdot v$$

$$v = F \cdot v$$

$a = \text{acceleration}$

$t = \text{time}$

$$[v] = [m^0 L^1 T^{-1}]$$

$$[u] = [m^0 L^1 T^{-1}]$$

$$\begin{aligned} [at] &= [a][t] \\ &= [m^0 L^1 T^{-2}][T] \\ &= [L^1 T^{-1}] \end{aligned}$$

Since dimensions of all terms of the equation are same. So the equation is dimensionally correct.

(2) check the correctness of $v^2 = u^2 + 2as$

$$\text{where } v = \beta \cdot v$$

$$[v^2] = [L^1 T^{-1}]^2 = [L^2 T^{-2}]$$

$$[u^2] = [L^1 T^{-1}]^2 = [L^2 T^{-2}]$$

$$[2as] = [a][s] = [L T^{-2}][L] = [L^2 T^{-2}]$$